

Approximation Based Reasoning and Conformant/Conditional Planning — Bridging Reasoning About Actions & Changes and Planning

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Reasoning about actions and changes (RAC)

Goal

How to represent actions and their effects? Reason about actions and their effects: **what will be true/false after the execution of an action (an action sequence) in a given state?** [▶ Illustration](#)

Activities

1. Development of **languages** for representing of dynamic domains (or actions and their effects)
2. Development of **basic algorithms** for computing successor states.
3. **Considering** of real-world domains (e.g. actions might have durations, non-deterministic, concurrent, etc.)

Important Notions

1. State
2. Algorithms for computing of successor states

Planning

Goal

Development of domain-independent planner(s) for **real-world applications**: computing a plan to achieve a predefined goal

Activities

1. Development of several domain-independent planners (the **algorithms for computing next state of the world** (RAC) ensures correctness)
2. Development of techniques to improve the **efficiency** and **scalability** of planners.

Important Considerations

1. Efficiency
2. Scalability

Planning

Realistic planning systems must be able to cope with

- ▶ incomplete information
- ▶ nondeterministic actions
- ▶ actions with durations
- ▶ actions that consume and produce resources
- ▶ deadlines of goals
- ▶ user preferences
- ▶ inconsistency of goals
- ▶ ...

Consequence

Each requirement represents a change in the “problem statement” for reasoning about actions and changes and/or planning.

RAC and Planning

Changes in problem statement (e.g. complete vs. incomplete initial state) lead to changes in

1. the notion of state (what is a state?) and/or
2. the basic algorithm (how to compute the successor state?)

in RAC and planning.

Hypothesis

New algorithms for computing the next state will be needed in planning with complex domains (e.g. actions with durations, resources, etc.).

Study in RAC will play important role in the new frontier of planning.

This tutorial: RAC in domains with static causal laws (state constraints) and planning with incomplete information and sensing actions.

Outline

Reasoning About Actions and Changes (RAC) and Planning

Incompleteness and Conformant Planning

Approximation Based Reasoning

Completeness Condition for Approximation Based Reasoning

Disjunctive Information

Incorporating Sensing Actions

Conclusions

Example [McCARTHY, 1959]

- ▶ *Problem*: John is at home and his car is at home also. He wants to go to the airport (going to Providence to attend ICAPS 2007).
- ▶ *Question*: What should John do?
- ▶ *Solution*: Drive to the airport.

Current Situation

This example can be encoded using any representation language developed for RAC and/or planning such as:

- ▶ situation calculus [McCARTHY & HAYES, 1969]
- ▶ event calculus [KOWALSKI & SERGOT, 1986]
- ▶ action languages [GELFOND & LIFSCHITZ, 1993]
- ▶ fluent calculus [THIELSCHER, 2000]
- ▶ STRIPS [FIKES & NILSON, 1971]
- ▶ PDDL [GHALLAB *et al.*, 1998]

Basic Ontologies (Situation Calculus, [McCARTHY & HAYES, 1969])

- ▶ **Situation**: a complete state of the universe in an instance of time, often given by a set of facts
 - ▶ The fact “John is at home” is represented by the atom $at(john, home)$.
 - ▶ “His car is at home also” is another fact, that can be represented by the atom $at(car, home)$.
- ▶ **Fluent**: a function whose domain is the space of situations
E.g. $at(john, home)$ is a Boolean function whose domain is the set of situations, $at(john, home)(s)$ is true says that “John is at home in situation s .”
- ▶ **Action**: causes for changes from situations to situations
E.g. $drive(home, airport)$ is an action that changes the situation in which John is at home to the situation in which John is at the airport.

Basic Ontologies (Situation Calculus, [REITER, 2001])

- ▶ **Situation**: a possible history of the world
 - ▶ s_0 – initial situation.
 - ▶ $do(drive(home, airport), s_0)$ – situation after the execution of $drive(home, airport)$ in s_0 .
- ▶ **Fluent**: a relation (a property of the world) whose (truth) value changes over time due to the execution of actions
 - ▶ $at(john, home)$ is a relation whose truth value changes – a *Boolean* fluent.
 - ▶ $number_paper(john)$ is a relation whose value changes – a *functional* fluent.
- ▶ **Action**: causes for *all* changes in the world
E.g. $drive(home, airport)$ is the *only action* that can change the world in our example.

Basic Ontologies (Action Languages, [GELFOND & LIFSCHITZ, 1993])

- ▶ **Actions** and **fluents** – same as in situation calculus in [REITER, 2001]
- ▶ **Fluent literal** – a fluent or its negation (a fluent preceeding by \neg)
E.g. $at(john, home)$, $\neg at(john, home)$
- ▶ **State**: two commonly used definitions
 - ▶ a set of fluents or
 - ▶ a *complete* and *consistent* set of fluent literals, i.e., s is a state if for every fluent f
 - ▶ either f or $\neg f$ belongs to s ; and
 - ▶ $\{f, \neg f\} \not\subseteq s$.

We will use the ontologies of action languages in this tutorial.

Action Language \mathcal{AL} — Syntax

- ▶ **Fluents**: propositional symbols (e.g. $at(john, home)$, $at(john, airport)$, $at(car, home)$, and $at(car, airport)$)
- ▶ **Actions**: propositional symbols (e.g. $drive(home, airport)$ and $drive(airport, home)$) disjoint from fluents
- ▶ **Laws**:
 - ▶ *Dynamic law*: describes effects of actions

$$drive(home, airport) \textbf{causes} at(john, airport), at(car, airport)$$
 - ▶ *Static causal law*: represents the relationship between fluents

$$\neg at(john, home) \textbf{if} at(john, airport)$$
 - ▶ *Executability law*: encodes the conditions under which an action can be executed

$$drive(home, airport) \textbf{executable} at(john, home), at(car, home)$$
 - ▶ *Initial state*: a set of fluent literals

Action Theory — Syntax

Definition

An **action theory** is a pair (\mathcal{D}, δ) where

- ▶ \mathcal{D} , called an *action domain*, is a set of dynamic, static causal, and executability laws.
- ▶ δ , called the *initial state*, is a set of fluent literals.

$(\mathcal{D}_a, \delta_a)$ —“Going to the Airport” Action Theory

$$\mathcal{D}_a = \left\{ \begin{array}{l} drive(home, airport) \textbf{executable} at(john, home), at(car, john) \\ drive(home, airport) \textbf{causes} at(john, airport), at(car, airport) \\ drive(airport, home) \textbf{executable} at(john, airport), at(car, airport) \\ drive(airport, home) \textbf{causes} at(john, home), at(car, home) \\ \neg at(john, airport) \textbf{if} at(john, home) \\ \neg at(car, airport) \textbf{if} at(car, home) \\ \neg at(john, home) \textbf{if} at(john, airport) \\ \neg at(car, home) \textbf{if} at(car, airport) \end{array} \right.$$

$$\delta_a = \{at(john, home), at(car, home), \neg at(john, airport), \neg at(car, airport)\}$$

$\mathcal{A}\mathcal{L}$ vs. PDDL (mostly a 1-1 correspondence, difference in static causal laws)

Domain: \mathcal{D}_a in PDDL representation

```
(define (domain airport)
  (:predicates (at ?x ?y)
    (location ?x) (person ?p) (car ?c))
  (:action drive
    :parameters (?x ?y)
    :precondition (and (location ?x) (location ?y)
      (person ?p) (at ?p ?x)
      (car ?c) (at ?c ?x))
    :effect (and (at ?c ?y) (at ?p ?y)
      (not (at ?c ?x)) (not (at ?p ?x))))))
```

Problem: δ_a and Goal in PDDL representation

```
(define (problem airport-1-1) (:domain airport)
  (:objects john car home airport)
  (:init person(john) car(car) location(home) location(airport)
    at(john,home) at(car,home))
  (:goal at(john,airport)))
```

$\mathcal{A}\mathcal{L}$ vs PDDL

$\mathcal{A}\mathcal{L}$	PDDL
Action	✓ Predicate
Fluent	✓ Precondition
Effect	Defined fluent or axiom
Executability condition	(no cyclic)
Static causal law (allow cyclic)	Typed Variables
Ground Instantiations (Variables: shorthand)	

Notes

1. Dealing directly with static causal laws is advantageous [THIEBAUX *et al.*, 2003].
2. Not many planners deal with static causal laws directly.

Fundamental Problems in RAC

- ▶ **The frame problem:** succinct representation of **what does not change** due to the execution of an action.
E.g. John's home does not change its location after John's drove his car to the airport.
- ▶ **The qualification problem:** encoding the conditions under which an action can be executed.
E.g. **Normally**, John can drive his car if he is at the same place as his car (Taken for granted: he has the key, his car will start, his car has enough gasoline, etc.)
- ▶ **The ramification problem:** accounting for **indirect effects** of actions.
E.g. If John's luggages are in his car then his luggages are at the airport after he executed the action of driving to the airport.

Current Situation

Adequate solutions for the above problems have been proposed in different formalisms for various settings.

Key Ideas in Solving the Fundamental Problems in RAC

- ▶ **The frame problem:** the law of inertia “normally, a fluent's value does not change” (successor state axioms — one per fluent (e.g. [REITER, 2001])).
- ▶ **The qualification problem:** encodes only the minimal requirement for the action to be executed.
- ▶ **The ramification problem:** causal law “things do not change by themselves; there must be a reason for a fluent literal to change its value.”

Action language \mathcal{AL} (Semantics) — Intuition

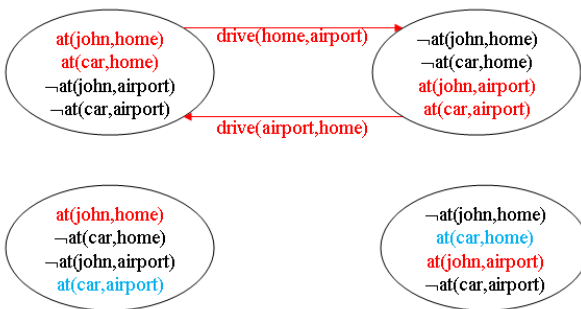
Given an action theory (\mathcal{D}, δ) , the action domain \mathcal{D} encodes a **transition system** consisting of elements of the form $\langle s_1, a, s_2 \rangle$ where s_1 and s_2 are states of the theory and a is an action that, when executed in s_1 , changes the state of the world from s_1 into s_2 . For example, in $(\mathcal{D}_a, \delta_a)$

$$\mathcal{D}_a = \left\{ \begin{array}{l} \text{drive}(\text{home}, \text{airport}) \text{ executable } \text{at}(\text{john}, \text{home}), \text{at}(\text{car}, \text{john}) \\ \text{drive}(\text{home}, \text{airport}) \text{ causes } \text{at}(\text{john}, \text{airport}), \text{at}(\text{car}, \text{airport}) \\ \text{drive}(\text{airport}, \text{home}) \text{ executable } \text{at}(\text{john}, \text{airport}), \text{at}(\text{car}, \text{airport}) \\ \text{drive}(\text{airport}, \text{home}) \text{ causes } \text{at}(\text{john}, \text{home}), \text{at}(\text{car}, \text{home}) \\ \neg \text{at}(\text{john}, \text{airport}) \text{ if } \text{at}(\text{john}, \text{home}) \\ \neg \text{at}(\text{car}, \text{airport}) \text{ if } \text{at}(\text{car}, \text{home}) \\ \neg \text{at}(\text{john}, \text{home}) \text{ if } \text{at}(\text{john}, \text{airport}) \\ \neg \text{at}(\text{car}, \text{home}) \text{ if } \text{at}(\text{car}, \text{airport}) \end{array} \right.$$

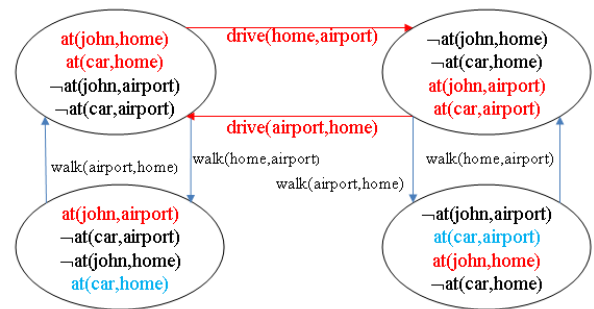
a transition is

$$\langle \{ \text{at}(\text{john}, \text{home}), \text{at}(\text{car}, \text{home}), \neg \text{at}(\text{john}, \text{airport}), \neg \text{at}(\text{car}, \text{airport}) \}, \\ \text{drive}(\text{home}, \text{airport}), \\ \{ \neg \text{at}(\text{john}, \text{home}), \neg \text{at}(\text{car}, \text{home}), \text{at}(\text{john}, \text{airport}), \text{at}(\text{car}, \text{airport}) \} \rangle$$

Example of States and Transitions



Going to the Airport



Adding the action $\text{walk}(X, Y)$

Action language \mathcal{AL} (Semantics) I

States in \mathcal{AL} theories

Let σ be a set of fluent literals.

σ **satisfies** a fluent literal l iff $l \in \sigma$ (denoted by $\sigma \models l$).

σ satisfies a set of fluent literals ψ iff $\psi \subseteq \sigma$ (denoted by $\sigma \models \psi$).

σ satisfies a static causal law φ **if** ψ if $\sigma \models \psi$ implies that $\sigma \models \varphi$.

$Cn_{\mathcal{D}}(\sigma)$, called the **closure** of σ , is the smallest set of literals that contains σ and satisfies all static causal laws in \mathcal{D} .

Note: $Cn_{\mathcal{D}}(\sigma)$ might be inconsistent.

Definition

A **state** of an action domain \mathcal{D} is a *complete* and *consistent* set of fluent literals which *satisfies all* static causal laws in \mathcal{D} (i.e., $s = Cn_{\mathcal{D}}(s)$ and s is consistent and complete).

Action language \mathcal{AL} (Semantics) II

Successor State

Given an action domain \mathcal{D} , a state s , and an action a .

- ▶ $de(a, s) = \{l \mid \mathcal{D} \text{ contains } a \text{ **causes** } l \text{ if } \varphi \text{ and } s \models \varphi\}$ is called the *direct effects* of a in s .
- ▶ s' is a **possible successor state** of s after the execution of a in s if

$$s' = Cn_{\mathcal{D}}(de(a, s) \cup (s \cap s'))$$

Intuition

- ▶ $s \cap s'$ – inertial part
- ▶ $de(a, s)$ – direct effects of a
- ▶ $s' \setminus (de(a, s) \cup (s \cap s'))$ – indirect effects of a

Example

Action language \mathcal{AL} (Semantics) III

For

$s_1 = \{at(john, home), at(car, home), \neg at(john, airport), \neg at(car, airport)\}$,

$s_2 = \{\neg at(john, home), \neg at(car, home), at(john, airport), at(car, airport)\}$

s_2 is a possible successor state of s_1 after the execution of

$drive(home, airport)$ in s_1 because

$$de(drive(home, airport), s_1) = \{at(john, airport), at(car, airport)\}$$

$$s_1 \cap s_2 = \emptyset$$

and

$$Cn_{\mathcal{D}_a}(de(drive(home, airport), s_1) \cup (s_1 \cap s_2)) = s_2$$

Transition Function — Φ

Action language \mathcal{AL} (Semantics) IV

$$\Phi : Actions \times States \rightarrow States$$

$$\Phi(a, s) = \begin{cases} \{s' \mid s' = Cn_{\mathcal{D}}(de(a, s) \cup (s \cap s'))\} \\ \text{if } \mathcal{D} \text{ contains an executability} \\ \text{law } a \text{ **executable** } \varphi \text{ and } s \models \varphi \\ \Phi(a, s) = \emptyset \text{ otherwise} \end{cases}$$

Definition

a is **executable** in s if $\Phi(a, s) \neq \emptyset$. (The transition $\langle s, a, s' \rangle$ denotes that $s' \in \Phi(a, s)$.)

Definition

Action language \mathcal{AL} (Semantics) V

For an action sequence $\alpha = a_1, \dots, a_n$ and a state s , the extended transition function $\hat{\Phi}$ is defined by

$$\hat{\Phi}(\alpha, s) = \begin{cases} \{s\} & n = 0 \\ \bigcup_{s' \in \hat{\Phi}(\alpha_{n-1}, s)} \Phi(a_n, s') & \text{if } a \text{ is executable in } \hat{\Phi}(\alpha_{n-1}, s) \end{cases}$$

α is **executable** in s if $\hat{\Phi}(\alpha, s) \neq \emptyset$.

Definition

(\mathcal{D}, δ) entails the query φ **after** α , denoted by $(\mathcal{D}, \delta) \models \varphi$ **after** α , if φ is true in every state belonging to $\hat{\Phi}(\alpha, \delta)$.

Bomb-In-The-Toilet Example

There may be a bomb in a package. Dunking the package into a toilet disarms the bomb. This action can be executed only if the toilet is not clogged. Flushing the toilet makes it unclogged.

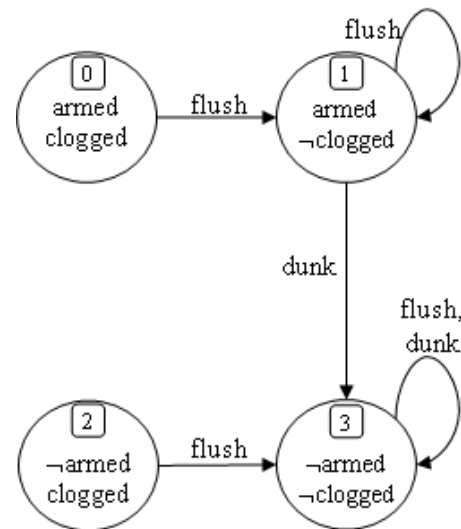
- ▶ Fluents: *armed, clogged*
- ▶ Actions: *dunk, flush*
- ▶ Action domain:

$$\mathcal{D}_b = \left\{ \begin{array}{l} \textit{dunk} \textbf{causes} \neg\textit{armed} \textbf{if} \textit{armed} \\ \textit{flush} \textbf{causes} \neg\textit{clogged} \\ \textit{dunk} \textbf{executable} \neg\textit{clogged} \\ \textit{flush} \textbf{executable} \textit{true}^* \end{array} \right\}$$

(* — present unless otherwise stated)

- ▶ Entailments

$$(\mathcal{D}_b, \{\textit{armed}, \textit{clogged}\}) \models \neg\textit{armed} \textbf{after} \langle \textit{flush}, \textit{dunk} \rangle$$



Dominoes Example

n dominoes $1, 2, \dots, n$ line up on the table such that if domino i falls down then $i + 1$ also falls down.

$$\mathcal{D}_d = \begin{cases} \text{down}(n + 1) \text{ if } \text{down}(n) \\ \text{touch}(i) \text{ causes } \text{down}(i) \end{cases}$$



It can be shown that

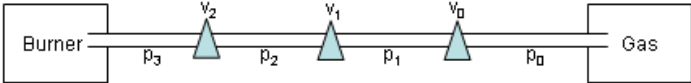
$$(\mathcal{D}_d, \delta_d) \models \text{down}(n) \text{ after } \text{touch}(i)$$

for every δ_d and i .

Gas Pipe

$n + 1$ sections of pipe (pressured/unpressured) connected through n valves (opened/closed) connects a gas tank to burner. A valve can be opened only if the valve on its right is closed. Closing a valve causes the pipe section on its right side to be unpressured. The burner will start a flame if the pipe section connecting to it is pressured. The gas tank is always pressured.

- ▶ Fluents: flame , $\text{opened}(V)$, $\text{pressured}(P)$, $0 \leq V \leq n$, $0 \leq P \leq n + 1$,
- ▶ Actions: $\text{open}(V)$, $\text{close}(V)$
- ▶ Action domain:

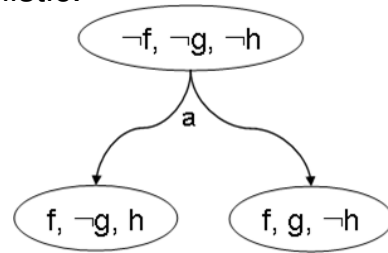


$$\mathcal{D}_g = \begin{cases} \text{open}(I) \text{ executable } \neg \text{opened}(I + 1) \\ \text{open}(I) \text{ causes } \text{opened}(I) \\ \text{close}(I) \text{ causes } \neg \text{opened}(I) \\ \text{pressured}(I + 1) \text{ if } \text{opened}(I), \text{pressured}(I) \\ \text{pressured}(0) \text{ if true} \\ \text{flame} \text{ if } \text{pressured}(n + 1) \end{cases}$$

Non-Deterministic \mathcal{AL} Theories

Action theories in \mathcal{AL} can be non-deterministic.

$$\mathcal{D}_n = \begin{cases} a \text{ causes } f \text{ if } \neg h, \neg g \\ h \text{ if } f, \neg g \\ g \text{ if } f, \neg h \end{cases}$$



Two successor states of $s_0 = \{\neg f, \neg g, \neg h\}$ after executing a :
 $s_1 = \{f, \neg g, h\}$ and $s_2 = \{f, g, \neg h\}$

Planning and Complexity (Complete Information)

Definition (Planning Problem)

- ▶ Given: an \mathcal{AL} -action theory (\mathcal{D}, δ) , where δ is a state of \mathcal{D} , and a set of fluent literals G .
- ▶ Determine: a sequence of actions α such that $(\mathcal{D}, \delta) \models G$ **after** α

From [LIBERATORE, 1997, TURNER, 2002]:

Theorem (Complexity)

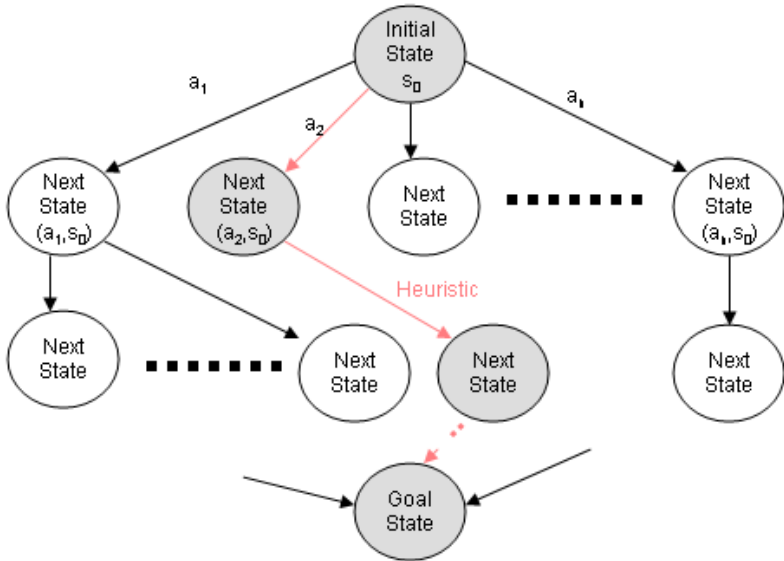
- ▶ (\mathcal{D}, δ) is **deterministic**: NP-hard even for plans of length 1, NP-complete for polynomial-bounded length plans (Classical Planning).
- ▶ (\mathcal{D}, δ) is **non-deterministic**: Σ_p^2 -hard even for plans of length 1, Σ_p^2 -complete for polynomial-bounded length plans (Conformant Planning in non-deterministic theories).

Planning Algorithms (Complete Information)

- (1) *Heuristic search based approaches*
 - ▶ State space: the search space is the set of possible states
 - ▶ Plan space (partial order planning): the search space is the set of possible plans
- (2) *Translation based approaches* (SAT-, model checking-, or answer set solvers).
 - ▶ SAT: translation into a SAT instance
 - ▶ Model checking: translation into a model checking problem
 - ▶ Answer set programming: translation into a logic program

Search Based Approaches

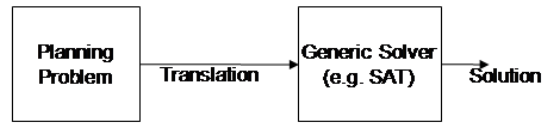
In search based planners, performance depends on how fast the search can be done \Rightarrow **accuracy of heuristic is the key.**



Heuristic Search Based Planners

Translation Based Approaches

In planners utilizing general theorem prover, performance depends on the performance of the general theorem prover.



Planning as Satisfiability

Pros and cons ((1) vs (2))

- ▶ (1) “independent” from the development in other communities, lots of good heuristics, easy to try out new heuristics
- ▶ (2) “dependent” from the development in other communities, heuristics are difficult to exploit in a systematic way
- ▶ (2) easier to deal with arbitrary domains than (1) (e.g. cyclic static causal laws)
- ▶ (2) easier to add “declarative domain knowledge”
- ▶ (2) easier to deal with “concurrent” actions than (1)

Reasoning About Actions and Changes (RAC) and Planning

Incompleteness and Conformant Planning

Approximation Based Reasoning

Completeness Condition for Approximation Based Reasoning

Disjunctive Information

Incorporating Sensing Actions

Conclusions

Approaches to Reasoning with Incomplete Information

Incomplete Information: initial state is not fully specified (e.g. δ in (\mathcal{D}, δ) might not be a state)

- ▶ Possible world approach (PSW): Extension of the transition function to a transition function over **belief states**.
- ▶ Approximation: Modifying the transition function to a transition function over **approximation states**.

Notation

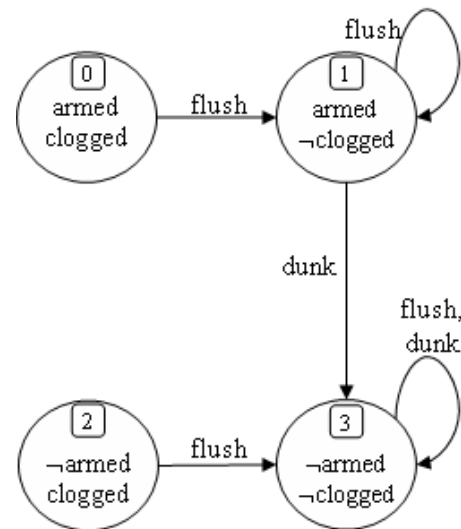
	Belief states (\mathcal{S} and Σ)	Approximation states (δ and Δ)	
\mathcal{S}	a set of states	a set of fluent literals	δ
Σ	a set of belief states	a set of approximation states	Δ

Example (Bomb-In-The-Toilet Revisited)

There may be a bomb in a package. Dunking the package into a toilet disarms the bomb. ...

- ▶ Fluents: *armed*, *clogged*
- ▶ Actions: *dunk*, *flush*
- ▶ Action domain:

$$\mathcal{D}_b = \begin{cases} \text{dunk} \text{ causes } \neg\text{armed} \text{ if } \text{armed} \\ \text{flush} \text{ causes } \neg\text{clogged} \\ \text{dunk} \text{ executable } \neg\text{clogged} \end{cases}$$



- ▶ Initially, we know nothing about the value of *armed* and *clogged*.
- ▶ **PWS**: the initial belief state $S_0 = \{0, 1, 2, 3\}$.
- ▶ **Approximation**: the initial approximation state $\delta_0 = \emptyset$.

Definitions

Approximation state/Partial state: a set of fluent literals which is a part of some state.

Belief state: a set of states

For an action theory (\mathcal{D}, δ_0) :

- ▶ Initial approximation state: δ_0 — a partial state
- ▶ Initial belief state:

$$S_0 = bef(\delta_0)$$

where

$$bef(\delta) = \{s \mid \delta \subseteq s, s \text{ is a state}\}$$

- ▶ A fluent formula φ true (false) in a belief state S if it true (false) in **every** state $s \in S$; it is unknown if it is neither true nor false in S .
- ▶ A fluent literal l is true (false) in an approximation state δ if $l \in \delta$ ($\neg l \in \delta$); unknown, otherwise. The truth value of a fluent formula φ is defined in the usual way.

Possible World Approach

▶ $S_0 = bef(\delta_0)$

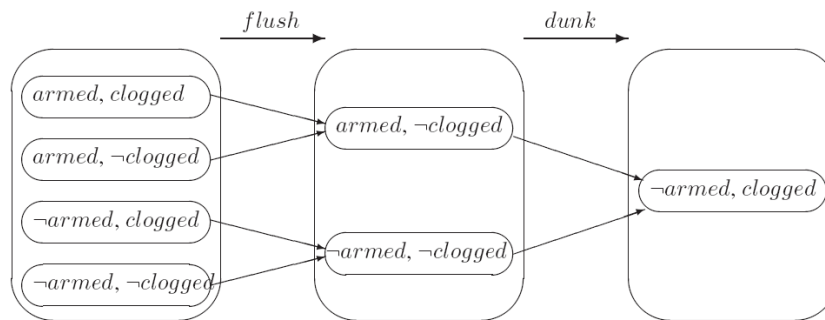
▶

$$\Phi^c(a, S) = \begin{cases} \emptyset & \text{if } a \text{ is not executable in some } s \in S \\ \bigcup_{s \in S} \Phi(a, s) & \text{otherwise} \end{cases}$$

▶ Φ^c extended to $\hat{\Phi}^c$ in the usual way

▶ $(\mathcal{D}, \delta_0) \models^P \varphi$ **after** α if φ is true in the final belief state

▶ Size of search space: n fluents $\rightarrow 2^{2^n}$ belief states



Conformant Planning and Complexity

Definition (Conformant Planning Problem)

- ▶ Given: an \mathcal{AL} -action theory (\mathcal{D}, δ) , where δ is a partial state, and a set of fluent literals G .
- ▶ Determine: a sequence of actions α such that $(\mathcal{D}, \delta) \models G$ **after** α

From [BARAL *et al.*, 2000, LIBERATORE, 1997, TURNER, 2002]:

Theorem (Complexity)

- ▶ **Conformant Planning**: (\mathcal{D}, δ) is deterministic: Σ_p^2 -hard even for plans of length 1, Σ_p^2 -complete for polynomial-bounded length plans.
- ▶ **Conformant Planning**: (\mathcal{D}, δ) is non-deterministic: Σ_p^3 -hard even for plans of length 1, Σ_p^3 -complete for polynomial-bounded length plans.

Planning Systems for Incomplete Domains

	DLV ^K	MBP	CMBP	SGP	POND	CFF	KACMBP
Language	<i>K</i>	<i>AR</i>	<i>AR</i>	PDDL	PDDL	PDDL	SMV
Sequential	yes	yes	yes	no	yes	yes	yes
Concurrent	yes	no	no	yes	no	no	no
Conformant	yes	yes	yes	yes	yes	yes	yes

Table: Features of Planning Systems

Planning Systems for Incomplete Domains

- ▶ Heuristic search based planners (search in the space of belief states)
 - ▶ CFF: A belief state S is represented by the initial belief state (a CNF formula) and the action sequence leading to S . To check whether a fluent literal l is true in S , a call to a SAT-solver is made. (subset of) PDDL as input.
 - ▶ POND: Graph plan based conformant planner. (subset of) PDDL as input.
- ▶ Translation into model checking: KACMBP (CMBP) – Input is a finite state automaton. Employing BDD (Binary Decision Diagram) techniques to represent and search the automaton. Consider nondeterministic domains with uncertainty in both the initial state and action effects.
- ▶ Translation into logic programming: DLV^K is a declarative, logic-based planning system built on top of the DLV system (an answer set solver).

Reasoning About Actions and Changes (RAC) and Planning

Incompleteness and Conformant Planning

Approximation Based Reasoning

Completeness Condition for Approximation Based Reasoning

Disjunctive Information

Incorporating Sensing Actions

Conclusions

General Considerations and Properties

- ▶ Address the complexity problem of the possible world approach:
give up completeness for efficiency in reasoning/planning
- ▶ Sound with respect to possible world semantics (formal proof is provided in some work)
- ▶ Representation languages and approaches are different
 - ▶ Situation calculus: [ETZIONI *et al.*, 1996, GOLDMAN & BODDY, 1994, PETRICK & BACCHUS, 2004]
 - ▶ Action languages:
[SON & BARAL, 2001, SON & TU, 2006, SON *et al.*, 2005b]
 - ▶ Logic programming: [SON *et al.*, 2005a]

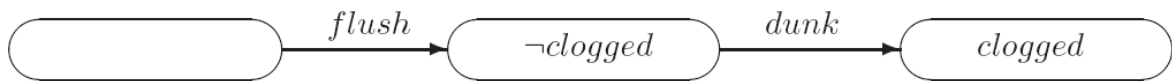
0-Approximation Approach [SON & BARAL, 2001]

- ▶ Initial partial state: δ_0
- ▶ Transition function is defined as

$$\Phi^0(a, \delta) = (\delta \cup de(a, \delta)) \setminus \neg pe(a, \delta)$$

where

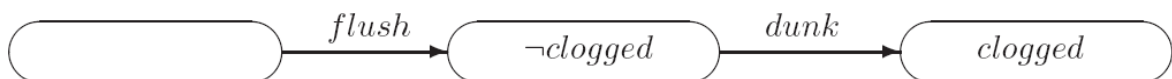
- ▶ $de(a, \delta)$ is the set of “direct effects” of a in δ
- ▶ $pe(a, \delta)$ is the set of “possible effects” of a in δ
- ▶ $(\mathcal{D}, \delta_0) \models^0 \varphi$ **after** α if φ is true in the final partial state
- ▶ n fluents $\rightarrow 3^n$ partial states
- ▶ Incomplete
- ▶ No static causal laws



0-Approximation Approach – Example

$$\mathcal{D}_b = \begin{cases} \text{dunk} \text{ causes } \neg\text{armed} \text{ if } \text{armed} \\ \text{flush} \text{ causes } \neg\text{clogged} \\ \text{dunk} \text{ executable } \neg\text{clogged} \end{cases}$$

- ▶ $\delta_0 = \emptyset$
 - ▶ dunk is not executable in δ_0
 - ▶ flush is executable in δ_0 , $de(\text{flush}, \delta_0) = pe(\text{flush}, \delta_0) = \{\neg\text{clogged}\}$
 - ▶ $\Phi^0(\text{flush}, \delta_0) = \{\neg\text{clogged}\}$
- ▶ $\delta_1 = \{\neg\text{clogged}\}$
 - ▶ $\text{dunk}, \text{flush}$ are executable in δ_1
 - ▶ $de(\text{dunk}, \delta_1) = \emptyset$ and $pe(\text{dunk}, \delta_1) = \{\neg\text{armed}\}$
 - ▶ $\Phi^0(\text{dunk}, \delta_1) = \{\text{clogged}\}$



Dealing with Static Causal Laws

How will the 0-approximation fare in the dominoes example?
 (Predictably: not so good!)



$$\mathcal{D}_d = \begin{cases} \text{down}(n + 1) \text{ if } \text{down}(n) \\ \text{touch}(i) \text{ causes } \text{down}(i) \end{cases}$$

$$\delta_0 = \emptyset$$

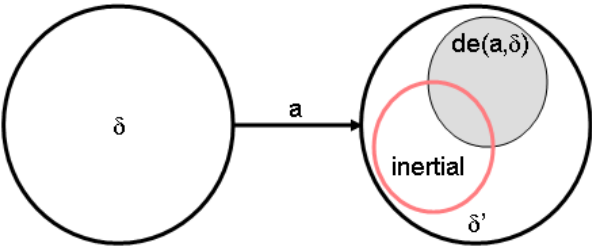
- ▶ $\text{touch}(i)$ is executable for every i
- ▶ $\text{de}(\text{touch}(i), \delta_0) = \{\text{down}(i)\}$ and $\text{pe}(\text{touch}(i), \delta_i) = \{\text{down}(i)\}$
- ▶ $\Phi^0(\text{touch}(i), \delta_0) = \{\text{down}(i)\}$

Intuitive result

$$\{\text{down}(j) \mid i \leq j \leq n\} \subseteq \Phi^0(\text{touch}(i), \delta_0)$$

Dealing with Static Causal Laws

$$\delta' = \text{Cn}_{\mathcal{D}}(\text{de}(a, \delta) \cup (\delta \cap \delta'))$$



The next state has three parts: (i) the direct effect $\text{de}(a, \delta)$; (ii) the inertial; (iii) the indirect effects (the closure of $\text{Cn}_{\mathcal{D}}$).

Dealing with Static Causal Laws

Question

What will be the inertial part?

Ideas

A literal does not change its value if it belongs to δ and

- ▶ **either** its negation cannot possibly hold in δ' ;
⇒ **possible holds approximation**
- ▶ **or** it cannot possibly change in δ'
⇒ **possible change approximation**

Φ^{ph} Approximation – Idea

A literal l **possibly holds** in the next state if

- ▶ it possibly holds in the current state (i.e., $l \notin \neg\delta$)
- ▶ it does not belong to the negation of the direct effect of the action (i.e., $l \notin \neg Cl_{\mathcal{D}}(de(a, \delta))$)
- ▶ there is some static causal law whose body possibly holds (i.e., there exists some static causal law l **if** φ such that φ possibly holds)

Φ^{ph} Approximation – Definition

$$E(a, \delta) = Cl_{\mathcal{D}}(e(a, \delta)) \quad [\text{always belongs to } \delta']$$

$$ph(a, \delta) = \bigcup_{i=0}^{\infty} ph^i(a, \delta) \quad [\text{possibly holds in } \delta']$$

$$ph^0(a, \delta) = (pe(a, \delta) \cup \{l \mid \neg l \notin \delta\}) \setminus \neg E(a, \delta)$$

OBS: if l **if** φ in \mathcal{D} and φ possibly holds then l possibly holds.

$$ph^{i+1}(a, \delta) = ph^i(a, \delta) \cup \left\{ l \mid \begin{array}{l} \exists [l \text{ if } \psi] \text{ in } \mathcal{D} \text{ s.t. } l \notin \neg E(a, \delta), \\ \psi \subseteq ph^i(a, \delta), \neg \psi \cap E(a, \delta) = \emptyset \end{array} \right\}$$

Definition

- ▶ if a is not executable in δ then

$$\Phi^{ph}(a, \delta) = \emptyset$$

- ▶ otherwise,

$$\Phi^{ph}(a, \delta) = Cl_{\mathcal{D}}(\{l \mid l \notin \neg ph(a, \delta)\})$$

Φ^{ph} Approximation – Example

$$\mathcal{D}_d = \left\{ \begin{array}{l} \text{down}(i+1) \text{ if } \text{down}(i) \\ \text{touch}(i) \text{ causes } \text{down}(i) \end{array} \right.$$

Computation for $\delta_0 = \emptyset$

- ▶ $de(\text{touch}(i), \delta_0) = \{\text{down}(i)\}$ and $pe(\text{touch}(i), \delta_0) = \{\text{down}(i)\}$
- ▶ $E(\text{touch}(i), \delta_0) = \{\text{down}(j) \mid i \leq j \leq n\}$
- ▶ $ph^0(\text{touch}(i), \delta_0) = \{\text{down}(j) \mid 1 \leq j \leq n\} \cup \{\neg \text{down}(j) \mid 1 \leq j < i\}$
- ▶ $ph^k(\text{touch}(i), \delta_0) = \{\text{down}(j) \mid 1 \leq j \leq n\} \cup \{\neg \text{down}(j) \mid 1 \leq j < i\}$
- ▶ $\Phi^{ph}(\text{touch}(i), \delta_0) = \{\text{down}(j) \mid i \leq j \leq n\}$

Φ^{pc} Approximation – Idea

A literal l **possibly changes** if

- ▶ it is not in δ
- ▶ it is a possible effect a (i.e., there exists a dynamic law a **causes** l **if** φ and φ is not false in δ)
- ▶ it is a possibly indirect effect of a (i.e., there exists a static causal law l **if** φ and φ possibly changes)

Φ^{pc} Approximation

$$pc(a, \delta) = \bigcup_{i=0}^{\infty} pc^i(a, \delta)$$

$$pc^0(a, \delta) = pe(a, \delta) \setminus \delta$$

$$pc^{i+1}(a, \delta) = pc^i(a, \delta) \cup \left\{ l \mid \begin{array}{l} \exists [l \text{ if } \psi] \in \mathcal{D} \text{ s.t. } , l \notin \delta \\ \psi \cap pc^i(a, \delta) \neq \emptyset, \text{ and } \neg\psi \cap E(a, \delta) = \emptyset \end{array} \right\}$$

Definition

- ▶ if a is not executable in δ then

$$\Phi^{pc}(a, \delta) = \emptyset$$

- ▶ otherwise,

$$\Phi^{pc}(a, \delta) = Cl_{\mathcal{D}}(E(a, \delta) \cup (\delta \setminus \neg pc(a, \delta)))$$

Φ^{pc} Approximation – Example

$$\mathcal{D}_d = \begin{cases} \text{down}(i+1) \text{ if } \text{down}(i) \\ \text{touch}(i) \text{ causes } \text{down}(i) \end{cases}$$

Computation for $\delta_0 = \emptyset$

- ▶ $de(\text{touch}(i), \delta_0) = \{\text{down}(i)\}$ and $pe(\text{touch}(i), \delta_0) = \{\text{down}(i)\}$
- ▶ $E(\text{touch}(i), \delta_0) = \{\text{down}(j) \mid i \leq j \leq n\}$
- ▶ $pc^0(\text{touch}(i), \delta_0) = \{\text{down}(i)\}$
- ▶ $pc^1(\text{touch}(i), \delta_0) = \{\text{down}(i), \text{down}(i+1)\}$
- ▶ $pc(\text{touch}(i), \delta_0) = \{\text{down}(j) \mid i \leq j \leq n\}$
- ▶ $\Phi^{pc}(\text{touch}(i), \delta_0) = \{\text{down}(j) \mid i \leq j \leq n\}$

Properties of Φ^{ph} and Φ^{pc} Approximations

- ▶ Behave exactly as 0-approximation in action theories without static causal laws
- ▶ Sound but incomplete (proofs in [TU, 2007])
- ▶ Support parallel execution of actions (formal proofs available)
- ▶ Incompatibility between Φ^{ph} and $\Phi^{pc} \Rightarrow$ could union the two to create a better approximation
- ▶ Deterministic: $\Phi^A(a, \delta)$ can be computed in polynomial-time
- ▶ Polynomial-length planning problem w.r.t Φ^A is NP-complete
- ▶ Could improve the approximations

Computing the Φ^{ph} Approximation

RESPH(\mathcal{D}, a, δ)
 INPUT: A domain description \mathcal{D} , an action a , and a partial state δ
 OUTPUT: $\Phi^{ph}(a, \delta)$

1. BEGIN
2. $de = \emptyset$ $pe = \emptyset$ $lit = \mathbf{F} \cup \neg\mathbf{F}$
4. **for each** dynamic causal law [a **causes** l **if** ψ] in \mathcal{D} **do**
5. **if** ψ possibly holds in δ **then**
6. $pe = pe \cup \{l\}$
7. **if** ψ holds in δ **then**
8. $de = de \cup \{l\}$
9. $E = \text{CLOSURE}(\mathcal{D}, de)$
10. $ph = (pe \cup (lit \setminus \neg\delta)) \setminus \neg E$
11. **repeat**
12. $stop = true$
13. **for each** static causal law [l **if** ψ] in \mathcal{D} **do**
14. **if** $l \notin \neg E$, $\psi \subseteq ph$, $\neg\psi \cap E = \emptyset$, and $l \notin ph$ **then**
15. $ph = ph \cup \{l\}$ $stop = false$
16. **until** $stop$
17. **return** $\text{CLOSURE}(\mathcal{D}, lit \setminus \neg ph)$
18. END

Figure: An algorithm for computing Φ^{ph}

Computing the Φ^{pc} Approximation

RESPC(\mathcal{D}, a, δ)
 INPUT: A domain description \mathcal{D} , an action a , and a partial state δ
 OUTPUT: $\Phi^{pc}(a, \delta)$

1. BEGIN
2. $de = \emptyset$ $pc = \emptyset$
3. **for each** dynamic causal law [a **causes** l **if** ψ] in \mathcal{D} **do**
4. **if** ψ possibly holds in δ **then**
5. **if** $l \notin \delta$ **then**
6. $pc = pc \cup \{l\}$
7. **if** ψ holds in δ **then**
8. $de = de \cup \{l\}$
9. $E = \text{CLOSURE}(\mathcal{D}, de)$
10. **repeat**
11. $stop = true$
12. **for each** static causal law [l **if** ψ] in \mathcal{D} **do**
13. **if** $\neg\psi \cap E = \emptyset$ and $\psi \cap pc \neq \emptyset$ and $l \notin \delta$ **then**
14. $pc = pc \cup \{l\}$ $stop = false$
15. **until** $stop$
16. **return** $\text{CLOSURE}(\mathcal{D}, E \cup (\delta \setminus \neg pc))$
17. END

Figure: An algorithm for computing $\Phi^{pc}(a, \delta)$

What is good about the approximation?

Theorem (Complexity)

Conformant Planning: (\mathcal{D}, δ) is deterministic: NP-complete for polynomial-bounded length plans.

Consequence

If (\mathcal{D}, δ) is complete, planners can use the 0-approximation (lower complexity) instead of the possible world semantics. In fact, classical planners can be used to solve conformant planning (change in the computation of the next state.)

Approximation Based Conformant Planners

- ▶ Earlier systems
[ETZIONI *et al.*, 1996, GOLDMAN & BODDY, 1994]: approximation is used in dealing with sensing actions (context-dependent actions and non-deterministic outcomes)
- ▶ PKS [PETRICK & BACCHUS, 2004] is very efficient (plus: use of domain knowledge in finding plans)
- ▶ CpA and CPASP [SON *et al.*, 2005b, SON *et al.*, 2005a] are competitive with others such as CFF, POND, and KACMBP in several benchmarks
- ▶ Incompleteness

Application in Conformant Planning

- ▶ CPASP:
 - ▶ Logic programming based
 - ▶ Uses Φ^{ph} approximation
 - ▶ Can generate both concurrent plans and sequential plans
 - ▶ Can handle disjunctive information about the initial state
 - ▶ Competitive with concurrent conformant planners and with others in problems with short solutions
- ▶ CPA:
 - ▶ Forward, best-first search with **simple** heuristic function (number of fulfilled subgoals)
 - ▶ Provides users with an option to select the approximation
 - ▶ Generates sequential plans only
 - ▶ Can handle disjunctive information about the initial state
 - ▶ Competitive with other state-of-the-art conformant planners

Experiments — Planning with concurrent actions I

Gas Pipe

Problem	\mathcal{C} -PLAN	DLV ^K	CPASP
Gaspip ^p (3)	-	0.08	0.40
Gaspip ^p (5)	-	0.17	0.75
Gaspip ^p (7)	-	0.44	1.22
Gaspip ^p (9)	-	17.44	3.17
Gaspip ^p (11)	-	-	8.83

Cleaner

Experiments — Planning with concurrent actions II

Problem	\mathcal{C} -PLAN	DLV ^K	CPASP
Cleaner ^p (2,2)	0.05	0.07	0.26
Cleaner ^p (2,5)	0.12	0.06	0.30
Cleaner ^p (2,10)	0.06	0.07	0.30
Cleaner ^p (4,2)	0.06	0.19	0.77
Cleaner ^p (4,5)	0.09	0.80	0.93
Cleaner ^p (4,10)	0.13	237.63	1.16
Cleaner ^p (6,2)	0.11	4.47	1.98
Cleaner ^p (6,5)	0.19	986.73	2.94
Cleaner ^p (6,10)	0.35	-	3.73

Bomb In The Toilet

Experiments — Planning with concurrent actions III

Problem	\mathcal{C} -PLAN	DLV ^K	CPASP
BT ^p (2,2)	0.07	0.07	0.11
BT ^p (4,2)	0.05	0.09	0.26
BT ^p (6,2)	1.81	3.06	0.34
BT ^p (8,4)	4.32	10.52	0.24
BT ^p (10,4)	-	-	1.91
BTC ^p (2,2)	0.05	0.05	0.13
BTC ^p (4,2)	0.07	0.90	0.30
BTC ^p (6,2)	7.51	333.27	0.67
BTC ^p (8,4)	-	-	0.50
BTC ^p (10,4)	-	-	1192.45

Experiments — Sequential Planning I

Cleaner

Problem	KACMBP	POND	CFF	CPA ^{ph}	CPA ^{pc}
Cleaner(2,5)	0.01	0.17	0.03	0.01	0.00
Cleaner(2,10)	0.08	0.85	0.07	0.03	0.02
Cleaner(2,20)	0.62	15.87	0.15	0.19	0.07
Cleaner(2,50)	13.55	-	0.80	2.76	0.92
Cleaner(2,100)	185.39	-	5.72	22.71	7.51
Cleaner(5,5)	0.01	1.46	0.11	0.07	0.04
Cleaner(5,10)	0.09	12.86	0.24	0.26	0.16
Cleaner(5,20)	7.82	214.83	0.85	1.78	0.88
Cleaner(5,50)	227.82	-	14.36	26.66	11.66
Cleaner(5,100)	-	-	-	214.27	92.81

Logistics

Experiments — Sequential Planning II

Problem	KACMBP	POND	CFF	CPA ^{ph}	CPA ^{pc}
Log(2,2,2)	0.19	1.11	0.03	0.15	0.16
Log(2,3,3)	355.96	11.89	0.06	8.95	9.543
Log(3,2,2)	2.10	4.02	0.06	11.87	4.54
Log(3,3,3)	29.8	24.66	0.12	409.68	435.55
Log(4,3,3)	-	40.12	0.14	-	-

Ring

Experiments — Sequential Planning III

Problem	KACMBP	POND	CFF	CPA ^{ph}	CPA ^{pc}
Ring(2)	0.00	0.15	0.06	0.00	0.00
Ring(3)	0.00	0.08	0.23	0.01	0.01
Ring(4)	0.00	0.25	3.86	0.02	0.02
Ring(5)	0.00	0.96	63.67	0.03	0.04
Ring(10)	0.02	-	-	1.01	1.05
Ring(15)	0.04	-	-	6.76	6.10
Ring(20)	0.15	-	-	27.44	22.68
Ring(25)	0.32	-	-	79.58	64.60

Bomb In The Toilet with Uncertainty

Experiments — Sequential Planning IV

Problem	KACMBP	POND	CFF	CPA ^{ph}	CPA ^{pc}
BTUC(10,1)	0.01	0.07	0.05	0.01	0.01
BTUC(20,1)	0.05	0.57	0.17	0.07	0.03
BTUC(50,1)	0.51	28.69	5.33	0.82	0.33
BTUC(100,1)	3.89	682.33	121.8	6.24	2.36
BTUC(10,5)	0.09	0.65	0.07	0.04	0.02
BTUC(20,5)	0.30	7.28	0.16	0.18	0.09
BTUC(50,5)	1.66	348.28	4.70	1.90	0.83
BTUC(100,5)	6.92	-	113.95	12.13	5.266
BTUC(10,10)	0.30	2.50	0.05	0.07	0.04
BTUC(20,10)	0.97	27.69	0.13	0.40	0.19
BTUC(50,10)	5.39	960.00	4.04	3.74	1.63
BTUC(100,10)	35.83	-	102.56	20.94	9.80

Domino

Experiments — Sequential Planning V

Problem	KACMBP	POND	CFF	CPA ^{ph}	CPA ^{pc}
Domino(10)	0.01	1.72	0.05	0.00	0.00
Domino(50)	0.27	-	4.44	0.00	0.00
Domino(100)	2.56	-	-	0.01	0.01
Domino(200)	29.10	-	-	0.02	0.02
Domino(500)	-	-	-	0.06	0.06
Domino(1000)	-	-	-	0.20	0.20
Domino(2000)	-	-	-	0.63	0.65
Domino(5000)	-	-	-	3.81	4.01

\mathcal{AL} vs. PDDL — Revisited

1. PDDL domains can be translated into \mathcal{AL} domains — 1-to-1
2. \mathcal{AL} domains can be translated into PDDL — might need to introduce additional actions (only polynomial number of actions)

Consequence

Planners using PDDL as their representation language can make use of the approximations.

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Conclusions

Motivation Example

- ▶ Action domain:

$$\mathcal{D}_b = \left\{ \begin{array}{l} \textit{dunk} \textbf{ causes } \neg\textit{armed} \textbf{ if } \textit{armed} \\ \textit{flush} \textbf{ causes } \neg\textit{clogged} \\ \textit{dunk} \textbf{ executable } \neg\textit{clogged} \end{array} \right\}$$

- ▶ Initial State: $\delta_0 = \emptyset$

- ▶ If δ_0 is splitted into $\Delta_1 = \{\{\textit{armed}\}, \{\neg\textit{armed}\}\}$ then

$$(\mathcal{D}_b, \Delta_1) \models^0 \neg\textit{armed} \textbf{ after } \langle \textit{flush}, \textit{dunk} \rangle$$

▶ See why?

- ▶ Splitting δ_0 into $\Delta_2 = \{\{\textit{clogged}\}, \{\neg\textit{clogged}\}\}$ does not help:

$$(\mathcal{D}_b, \Delta_2) \not\models^0 \neg\textit{armed} \textbf{ after } \langle \textit{flush}, \textit{dunk} \rangle$$

▶ See why?

Questions

Given an action theory (\mathcal{D}, δ_0) and a fluent formula φ ,

- ▶ **When \models^0 is complete?**, i.e., when

$$(\mathcal{D}, \delta_0) \models^P \varphi \text{ after } \alpha \Leftrightarrow (\mathcal{D}, \delta_0) \models^0 \varphi \text{ after } \alpha$$

for every sequence of actions α ?

- ▶ **How to make it complete?** what fluents whose values need to be considered in the beginning in order for 0-approximation to be complete?

Why important?

- ▶ If \models^0 is complete then the 0-approximation can be used instead of the possible world approach (reasoning process does not need to examine all possible initial states of the domain.)
- ▶ If \models^0 is incomplete then (\mathcal{D}, δ_0) can be transformed into a complete one.

When is \models^0 complete?

$(\mathcal{D}, \delta_0) \models \varphi \text{ after } \alpha$?

- ▶ Possible World Approach: Our knowledge is a belief state (set of possible states) $bel(\delta_0)$
- ▶ 0-approximation: Our knowledge is a partial state δ

Basic Idea

Characterize when reasoning with $bel(\delta_0)$ is the same as reasoning with δ (w.r.t. φ) — δ provides enough knowledge for reasoning about φ .

▶ [Illustration](#)

Approach

- ▶ **Dependency** \triangleleft between literals: $l \triangleleft g$ implies that to reason about l , may need to know g
- ▶ **Reducibility**: $S \ggg_{\varphi} \delta$ if there exists a state $s \in S$ such that φ does not depend on $s \setminus \delta$

Dependencies and Reducibility I

- ▶ A literal l **depends on** a literal g , written as $l \triangleleft g$, if
 - ▶ $l = g$ or $\neg l \triangleleft \neg g$, or
 - ▶ there exists a **causes** l **if** ψ such that $g \in \psi$, or
 - ▶ there exists $l \triangleleft h$ and $h \triangleleft g$.
- ▶ An action a **depends on** a literal l , written as $a \triangleleft l$, if either
 - ▶ there exists a **executable** ψ such that $\neg l \in \psi$, or
 - ▶ there exists a literal g such that $a \triangleleft g$ and $g \triangleleft l$.

Example

$$\mathcal{D}_b = \left\{ \begin{array}{l} \text{dunk} \text{ causes } \neg \text{armed} \text{ if } \text{armed} \\ \text{dunk} \text{ causes } \text{clogged} \\ \text{flush} \text{ causes } \neg \text{clogged} \\ \text{dunk} \text{ executable } \neg \text{clogged} \end{array} \right\}$$

- ▶ $\neg \text{armed} \triangleleft \neg \text{armed}$ as \triangleleft is reflexive
- ▶ $\neg \text{armed} \triangleleft \text{armed}$ because of the first statement

Dependencies and Reducibility II

- ▶ A disjunction $\gamma = l_1 \vee \dots \vee l_n$ depends on a literal g , written as $\gamma \triangleleft g$, if there exists some l_i such that $l_i \triangleleft g$.
- ▶ A belief state S is **reducible** to δ w.r.t. $\varphi = \gamma_1 \wedge \dots \wedge \gamma_n$, denoted by $S \gg_{\varphi} \delta$ if
 - ▶ δ is a subset of every state s in S ,
 - ▶ for $1 \leq i \leq n$, there exists a state $s \in S$ such that $\gamma_i \not\triangleleft (s \setminus \delta)$, and
 - ▶ for any action a , there exists a state $s \in S$ such that $a \not\triangleleft (s \setminus \delta)$.

Example

- ▶ For $\delta = \{\text{clogged}\}$ (or $\{\neg \text{clogged}\}$), $\text{bef}(\delta) \not\gg_{\neg \text{armed}} \delta$ as $\neg \text{armed} \triangleleft s \setminus \delta$ for every $s \in \text{bef}(\delta)$
- ▶ But, for $\delta = \{\text{armed}\}$ (or $\{\neg \text{armed}\}$), $\text{bef}(\delta) \gg_{\neg \text{armed}} \delta$ as $\neg \text{armed} \not\triangleleft s \setminus \delta$ for some $s \in \text{bef}(\delta)$ (e.g. $s = \{\text{clogged}, \text{armed}\}$).

Example (Summary)

$$\mathcal{D}_b = \left\{ \begin{array}{l} \text{dunk} \textbf{causes} \neg\text{armed} \textbf{if} \text{armed} \\ \text{dunk} \textbf{causes} \text{clogged} \\ \text{flush} \textbf{causes} \neg\text{clogged} \\ \text{dunk} \textbf{executable} \neg\text{clogged} \end{array} \right\}$$

► Dependencies:

- $\neg\text{armed} \triangleleft \neg\text{armed}$
- $\neg\text{armed} \triangleleft \text{armed}$

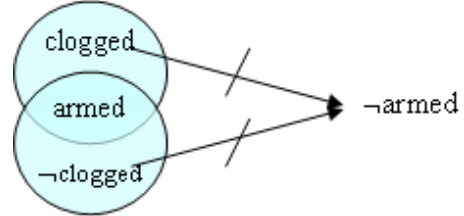
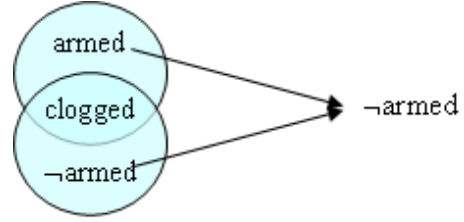
► Reducibility:

- For $\delta = \{\text{clogged}\}$ (or $\{\neg\text{clogged}\}$),

$$\text{bef}(\delta) \not\gg_{\neg\text{armed}} \delta$$

- But, for $\delta = \{\text{armed}\}$ (or $\{\neg\text{armed}\}$)

$$\text{bef}(\delta) \gg_{\neg\text{armed}} \delta$$



Condition for Completeness of 0-approximation

Theorem

Let (\mathcal{D}, δ_0) be an action theory without static causal laws and φ be a fluent formula. If $\text{bef}(\delta_0) \gg_{\varphi} \delta_0$ then for every sequence of actions α ,

$$(\mathcal{D}, \delta_0) \models^P \varphi \textbf{ after } \alpha \Leftrightarrow (\mathcal{D}, \delta_0) \models^0 \varphi \textbf{ after } \alpha$$

Examples

- Cannot say whether $(\mathcal{D}_1, \{\{\text{clogged}\}\}) \models^P \neg\text{armed} \textbf{ after } \alpha$ iff $(\mathcal{D}_1, \{\{\text{clogged}\}\}) \models^0 \neg\text{armed} \textbf{ after } \alpha$ for every α as $\text{bef}(\{\text{clogged}\}) \not\gg_{\neg\text{armed}} \{\text{clogged}\}$
- But, $(\mathcal{D}_1, \{\{\text{armed}\}\}) \models^P \neg\text{armed} \textbf{ after } \alpha$ iff $(\mathcal{D}_1, \{\{\text{armed}\}\}) \models^0 \text{armed} \textbf{ after } \alpha$ for every α as $\text{bef}(\{\text{armed}\}) \gg_{\neg\text{armed}} \{\text{armed}\}$

How to make \models^0 complete?

- ▶ **Basic Idea:** find a set of fluents F , called **decisive set**, to split δ_0 into Δ_0 such that for each $\delta \in \Delta_0$,

$$bef(\delta) \gg_{\varphi} \delta$$

as by the completeness theorem, this guarantees

$$(\mathcal{D}, \delta_0) \models^P \varphi \text{ after } \alpha \Leftrightarrow (\mathcal{D}, \Delta_0) \models^0 \varphi \text{ after } \alpha$$

- ▶ Example: $\{armed\}$ is a decisive set for \emptyset w.r.t. $\varphi = \neg armed$ but $\{clogged\}$ is not
- ▶ We developed an algorithm for computing such a decisive set
 - ▶ based on analyzing dependency relationships
 - ▶ most of the time returns a minimal one
 - ▶ runs in polynomial time

Computing A Decisive Set

Algorithm

DECISIVE($(\mathcal{D}, \delta_0), \varphi$)

INPUT: an action theory (\mathcal{D}, δ_0) and a formula $\varphi = \gamma_1 \wedge \dots \wedge \gamma_n$

OUTPUT: a decisive set for δ_0 w.r.t. φ

1. BEGIN
2. $F = \emptyset$
3. compute dependencies between literals
4. compute dependencies between actions and literals
5. **for** each fluent f unknown in δ_0 **do**
6. **if** there exists $1 \leq i \leq n$ s.t. γ_i depends on both f and $\neg f$ or
7. an action a s.t. a depends on both f and $\neg f$
8. **then** $F = F \cup \{f\}$
9. **return** F ;
10. END

Dealing with Static Causal Laws

Definition

Let \mathcal{D} be an action domain. A fluent literal l **depends on** a fluent literal g , written as $l \triangleleft g$, if and only if one of the following conditions holds.

1. $l = g$
2. \mathcal{D} contains a dynamic causal law $[a \text{ causes } l \text{ if } \psi]$ such that $g \in \psi$.
3. \mathcal{D} contains a static causal law $[l \text{ if } \psi]$ such that $g \in \psi$.
4. There exists a fluent literal h such that $l \triangleleft h$ and $h \triangleleft g$.
5. The complement of l depends on the complement of g , i.e., $\neg l \triangleleft \neg g$.

Completeness Condition for Simple Theories

A belief state S is **reducible** to δ w.r.t. $\varphi = \gamma_1 \wedge \dots \wedge \gamma_n$, denoted by $S \ggg_{\varphi} \delta$ if

- ▶ δ is a subset of every state s in S ,
- ▶ for $1 \leq i \leq n$, there exists a state $s \in S$ such that $\gamma_i \not\triangleleft (s \setminus \delta)$, and
- ▶ for any action a , there exists a state $s \in S$ such that $a \not\triangleleft (s \setminus \delta)$.

Definition

An action theory (\mathcal{D}, δ_0) is *simple* if every static causal law in \mathcal{D} is of the form $l \text{ if } g$.

Theorem

Let (\mathcal{D}, δ_0) be a simple action theory and φ be a fluent formula. If $\text{bef}(\delta_0) \ggg_{\varphi} \delta_0$ then for every sequence of actions α ,

$$(\mathcal{D}, \delta_0) \models^P \varphi \text{ after } \alpha \Leftrightarrow (\mathcal{D}, \delta_0) \models^0 \varphi \text{ after } \alpha$$

Reasoning with disjunctive information

Reasoning with disjunctive information can be done similar to reasoning in the presence of incomplete information since the knowledge of a reasoner can be represented by a belief states.

- ▶ Not a problem with reasoning but representation for possible world approach \Rightarrow compact representation of the initial belief state or belief states during the reasoning process is useful (e.g. CFF)
- ▶ For approximation based reasoning: compacting a belief state into a single partial state causes losing of information \Rightarrow expansion into set of partial states if completeness is required (e.g. CpA)
- ▶ Completeness condition still holds

Bomb-In-The-Toilet Domain

Problem	KACMBP	POND	CFF	CPA ⁺
Bomb(5,1)	0.00	0.03	0.03	0.00
Bomb(10,1)	0.01	0.07	0.05	0.00
Bomb(20,1)	0.05	0.57	0.17	0.03
Bomb(50,1)	0.51	28.69	5.33	0.31
Bomb(100,1)	3.89	682.33	121.8	2.28
Bomb(5,5)	0.04	0.10	0.04	0.00
Bomb(10,5)	0.09	0.65	0.07	0.02
Bomb(20,5)	0.30	7.28	0.16	0.07
Bomb(50,5)	1.66	348.28	4.70	0.68
Bomb(100,5)	6.92	-	113.95	4.50
Bomb(5,10)	0.11	0.35	0.03	0.01
Bomb(10,10)	0.30	2.50	0.05	0.05
Bomb(20,10)	0.97	27.69	0.13	0.15
Bomb(50,10)	5.39	960.00	4.04	1.26
Bomb(100,10)	35.83	-	102.56	7.44

Reasoning About Actions and Changes (RAC) and Planning

Incompleteness and Conformant Planning

Approximation Based Reasoning

Completeness Condition for Approximation Based Reasoning

Disjunctive Information

Incorporating Sensing Actions

Conclusions

Why sensing actions?

- ▶ Some properties of the domain can be observed after some **sensing actions** are executed
 - ▶ Cannot decide whether a package contains a bomb until we use a special device to detect it
 - ▶ A robot cannot determine an obstacle until it uses a sensor to detect it
- ▶ Two important questions:
 - ▶ What is a plan?
 - ▶ How to reason about sensing actions?

Extending \mathcal{AL} to handle sensing actions

- ▶ Allow knowledge-producing laws of the form

a **determines** θ

“if sensing action a is executed, then the values of $l \in \theta$ will be known”

- ▶ New language is called $\mathcal{AL}_{\mathcal{K}}$

Why sensing actions? — Example

- ▶ One bomb, two packages; exactly one package contains the bomb
- ▶ Initially, the toilet is not clogged. No *flush* action.
- ▶ Bomb can be detected by only by *X-ray*.

$$\mathcal{D}_2 = \left\{ \begin{array}{l} \mathbf{oneof} \{armed(1), armed(2)\} \\ dunk(P) \mathbf{causes} \neg armed(P) \\ dunk(P) \mathbf{causes} clogged \\ \mathbf{impossible} \text{ } dunk(P) \mathbf{if} \text{ } clogged \\ x\text{-ray} \mathbf{determines} \{armed(1), armed(2)\} \end{array} \right\}$$

- ▶ No conformant plan for

$$\mathcal{P}_1 = (\mathcal{D}_2, \{\neg clogged\}, \{\neg armed(1), \neg armed(2)\})$$

What is a plan in the presence of sensing actions?

- ▶ **Conditional Plans**: take into account contingencies that may arise
 - ▶ If a is a non-sensing action and $\langle \beta \rangle$ is a conditional plan then $\langle a, \beta \rangle$ is a conditional plan
 - ▶ If a is a sensing action that senses literals l_1, \dots, l_n , and $\langle \beta_i \rangle$ is a conditional plan then

$$\left\langle a, \mathbf{cases} \begin{pmatrix} l_1 \rightarrow \beta_1 \\ \dots \\ l_n \rightarrow \beta_n \end{pmatrix} \right\rangle$$

is a conditional plan

Example of Conditional Plan

$$\left\langle x\text{-ray}, \mathbf{cases} \begin{pmatrix} \mathit{armed}(1) \rightarrow \mathit{dunk}(1) \\ \mathit{armed}(2) \rightarrow \mathit{dunk}(2) \end{pmatrix} \right\rangle$$

is a solution of

$$\mathcal{P}_1 = (\mathcal{D}_2, \{\neg \mathit{clogged}\}, \{\neg \mathit{armed}(1), \neg \mathit{armed}(2)\})$$

How to reason about sensing actions?

- ▶ Must take into account different outcomes of sensing actions
 - ▶ Transition function: $Actions \times Partial\ States \rightarrow \mathcal{2}^{Partial\ States}$
- ▶ For each $A \in \{ph, pc\}$, we define a transition function Φ_S^A as follows
 - ▶ for a non-sensing action a , Φ_S^A is the same as Φ^A
 - ▶ for a sensing action a , each partial state in Φ_S^A corresponds to a literal that is sensed by a
- ▶ Result in four different approximations of \mathcal{AL}_K domain descriptions
- ▶ Entailment \models_S^A
 $(\mathcal{D}, \delta_0) \models_S^A \varphi$ **after** α
if φ is true in every final partial state of the execution of α
- ▶ Properties
 - ▶ Φ_S^A can be computed in polynomial time
 - ▶ the polynomial-length conditional planning: NP-complete

\mathcal{AL}_K Approximations

Definition

- ▶ If a is not executable in δ then
$$\Phi_S^A(a, \delta) = \emptyset$$
- ▶ If a is a non-sensing action then
$$\Phi_S^A(a, \delta) = \begin{cases} \emptyset & \text{if } \Phi^A(a, \delta) \text{ is consistent} \\ \{\Phi^A(a, \delta)\} & \text{otherwise} \end{cases}$$
- ▶ If a is a sensing action associated with
 a **determines** θ
then
$$\Phi_S^A(a, \delta) = \{Cl_{\mathcal{D}}(\delta \cup \{g\}) \mid g \in \theta \text{ and } Cl_{\mathcal{D}}(\delta \cup \{g\}) \text{ is consistent}\}$$

Application in Conditional Planning

- ▶ **Conditional Planning Problem:** $\mathcal{P} = (\mathcal{D}, \delta_0, \mathcal{G})$

A solution of \mathcal{P} is a conditional plan α such that

$$(\mathcal{D}, \delta_0) \models^P \mathcal{G} \text{ after } \alpha$$

- ▶ ASCP:
 - ▶ Implemented in logic programming
 - ▶ Approximation: Φ_S^{pc}
 - ▶ Can generate both concurrent plans and sequential plans
 - ▶ Soundness and completeness of ASCP are proved
 - ▶ Competitive with some other conditional planners

Experiments

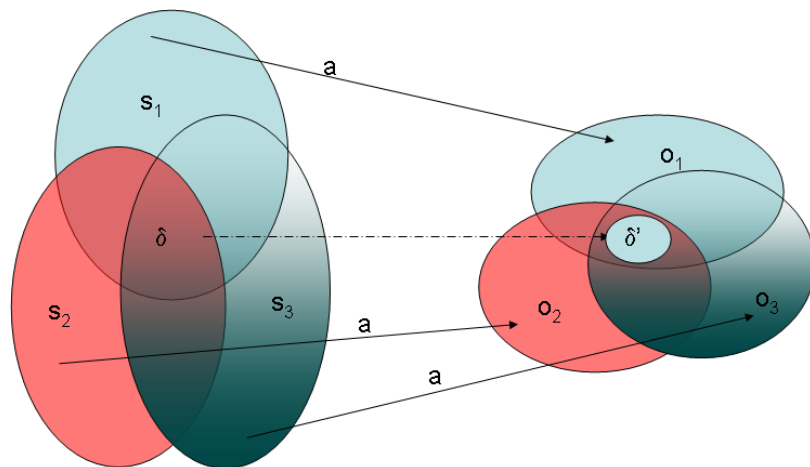
Problem	Min. Plan	ASCP		SGP	POND	MBP
		cmodels	smodels			
BTS1(4)	4x4	0.808	1.697	0.22	0.189	0.048
BTS1(6)	6x6	5.959	83.245	2.44	0.233	0.055
BTS1(8)	8x8	25.284	-	24.24	0.346	0.076
BTS1(10)	10x10	85.476	-	-	0.918	0.384
BTS2(4)	4x4	1.143	3.858	0.32	0.198	0.067
BTS2(6)	6x6	19.478	1515.288	3.23	0.253	2.163
BTS2(8)	8x8	245.902	-	25.5	0.452	109.867
BTS2(10)	10x10	345.498	-	-	1.627	178.823
BTS3(4)	4x4	1.099	5.329	0.44	0.195	1.93
BTS3(6)	6x6	7.055	-	3.89	0.258	147.76
BTS3(8)	8x8	56.246	-	28.41	0.549	-
BTS3(10)	10x10	248.171	-	-	2.675	-
BTS4(4)	4x4	1.696	3.556	0.64	0.191	-
BTS4(6)	6x6	13.966	149.723	4.92	0.264	-
BTS4(8)	8x8	115.28	-	30.34	0.708	-
BTS4(10)	10x10	126.439	-	-	4.051	-

Table: Performance of ASCP on the Bomb domains

Lessons Learned

1. Study in reasoning about actions and changes might provide useful ways for dealing with planning in complex domains
2. Approximations can compensate for the inaccuracy of heuristics
3. Approximations can be useful when the computation of the next state is more complicated
4. Completeness conditions can be used to deal with sensing actions in conditional planners: deciding when to execute a sensing action?

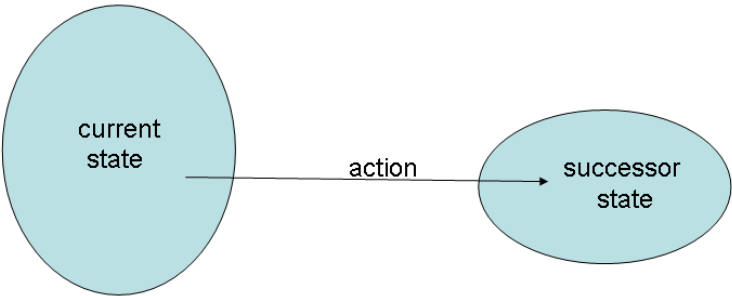
Intuition



$$\delta' = \Phi^0(a, \delta) \subseteq \Phi(a, s_1) \cap \Phi(a, s_2) \cap \Phi(a, s_3) = \Omega$$

$l \in \Omega \setminus \delta' \rightarrow l$ 'depends' on something in $s_1 \setminus \delta$ or $s_2 \setminus \delta$ or $s_3 \setminus \delta$

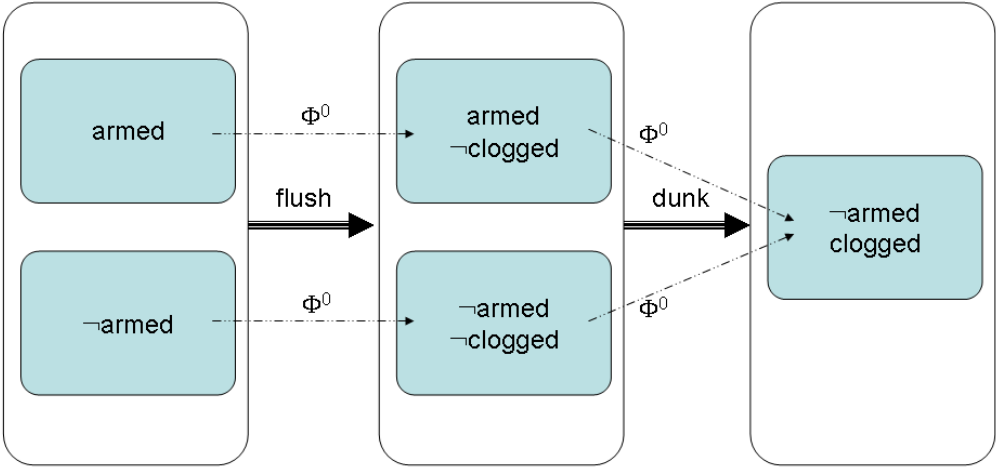
Illustration



- 1. *Representation*: how to represent actions and their effects?
- 2. *Reasoning*: how to compute the successor state(s)?

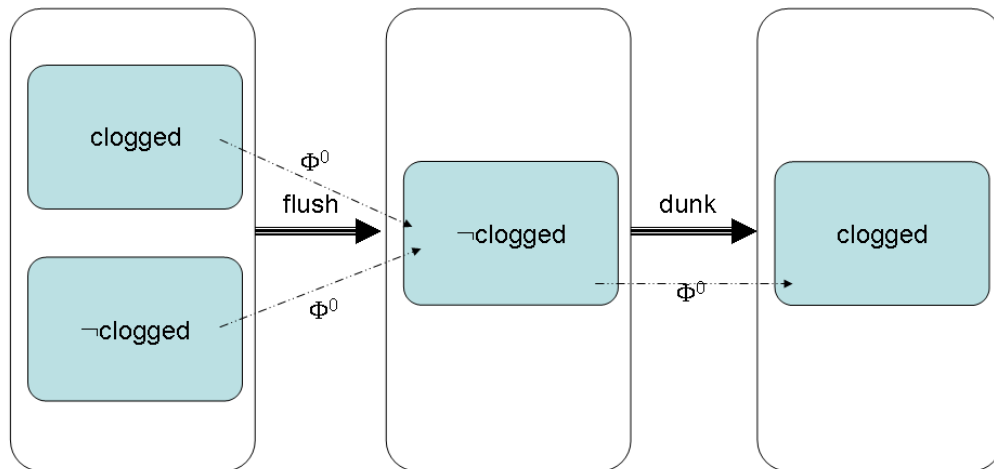
▶ Return

Splitting \emptyset to $\{armed\}$ and $\{\neg armed\}$ works



▶ Return

Splitting \emptyset to $\{clogged\}$ and $\{\neg clogged\}$ does not work







Lack of information about **armed** prevents the 0-approximation in reaching the conclusion

▶ Return


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